

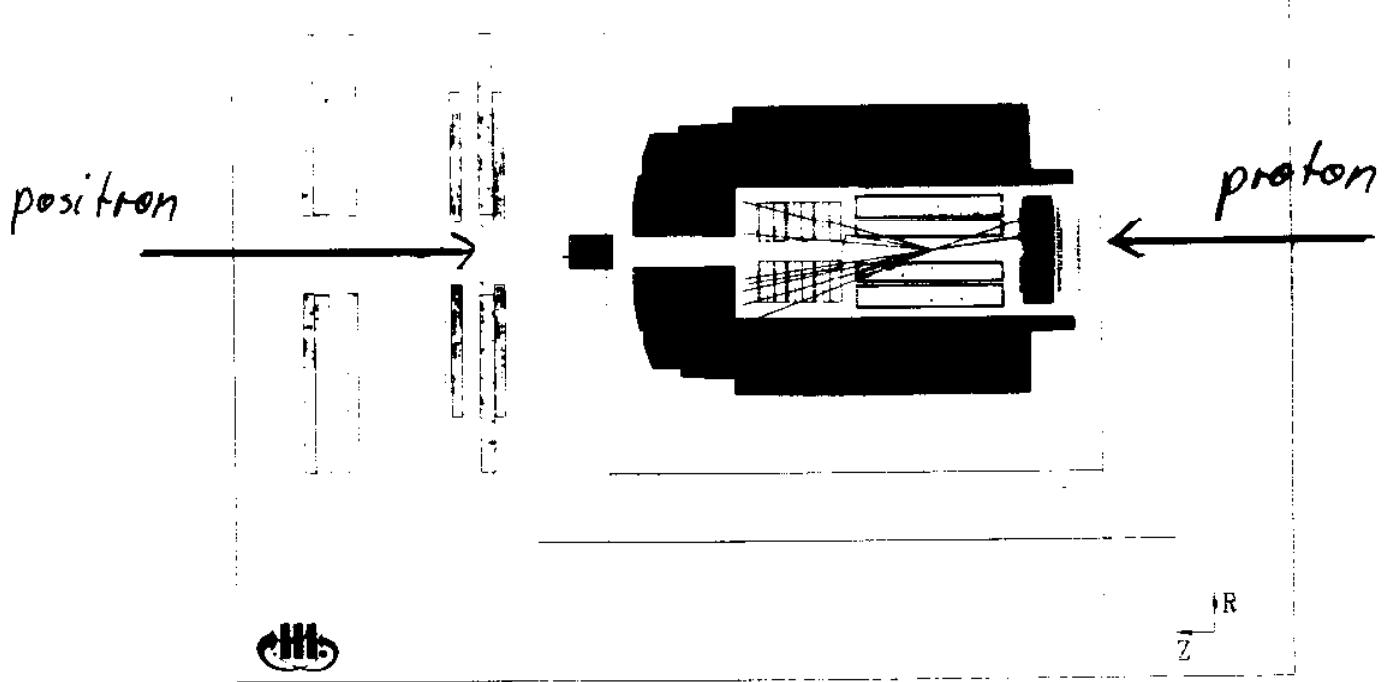
# Measurement and Interpretation of $F_2^{D(3)}(x_{IP}, \beta, Q^2)$

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for the H1 Collaboration

- Brief description of the H1-detector
- Kinematics of diffraction
- Measurement of  $F_2^{D(3)}(x_{IP}, \beta, Q^2)$
- Factorisation breaking
- Measurement of  $\tilde{F}_2^D(\beta, Q^2)$
- QCD-analysis of  $\tilde{F}_2^D(\beta, Q^2)$
- Summary and Conclusions

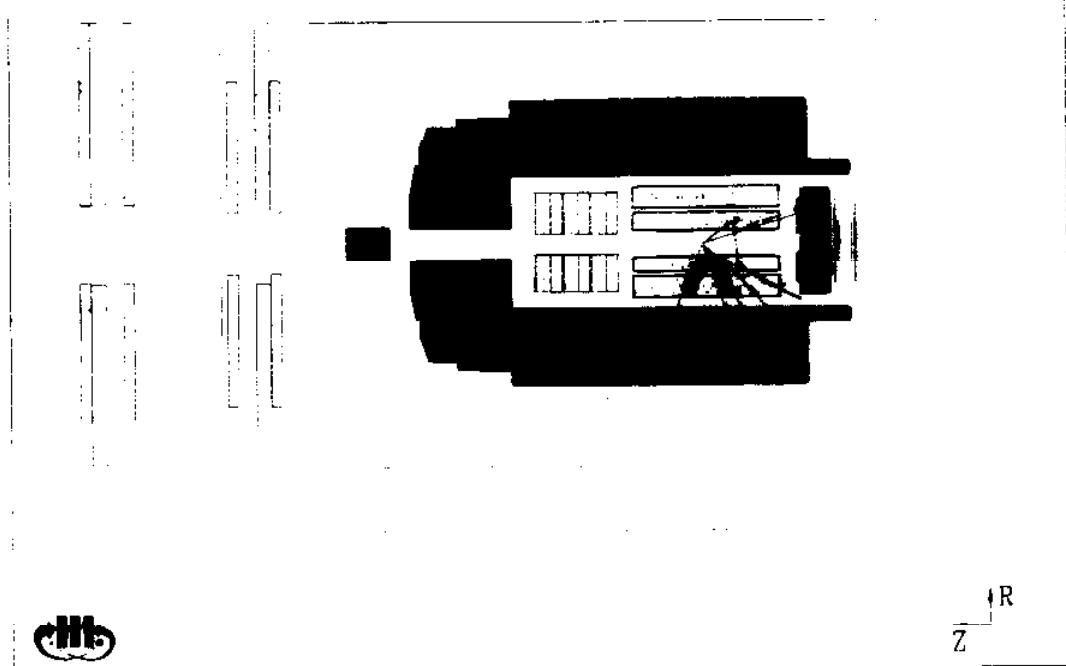
 Run 64901 Event 33275 Class 3 10 1 26 28 Date 13/07/1994

## "standard"-DIS



 Run 63718 Event 44072 Class: 3 10 11 16 17 26 Date 13/07/1994

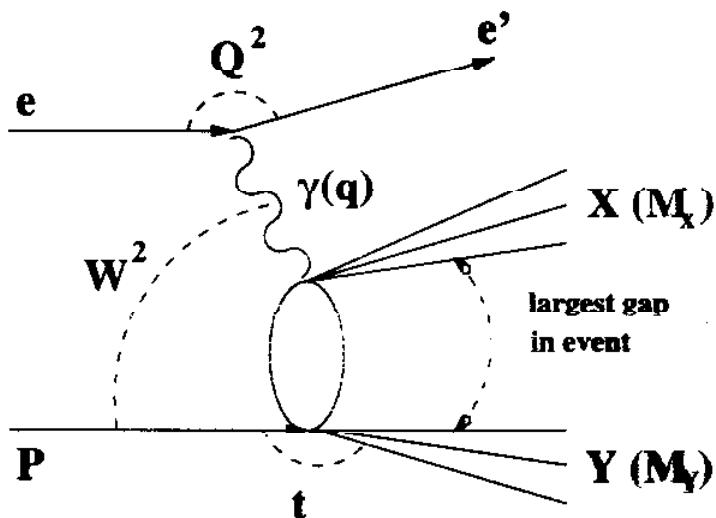
## diffractive



# Diffraction at HERA

"standard" kinematic variables for DIS:

$$Q^2 = -q^2 ; \quad x_{Bj} = \frac{Q^2}{2P \cdot q} ; \quad y = \frac{q \cdot P}{e \cdot P} ; \quad W^2 = (q + P)^2$$



additional variables in terms of systems X and Y:

$$\beta = \frac{Q^2}{2q \cdot (P-Y)} \approx \frac{Q^2}{Q^2 + M_X^2} \Rightarrow x_{Bj} = \beta \cdot x_P$$

$$x_P = \frac{q \cdot (P-Y)}{q \cdot P} \approx \frac{Q^2 + W^2}{Q^2 + M_X^2}$$

definitions are applicable to ANY type of process

interpretation in terms of exchange :

- $x_P$  momentum fraction of exchange particle
- $\beta$  momentum fraction of parton

## Definition of Cross Section

diffractive events are selected by requiring:

a gap in pseudorapidity ( $\eta = -\ln \tan(\frac{\Theta}{2})$ )  
between 7.5 and 3.4 ( $< 3.5^\circ$ )

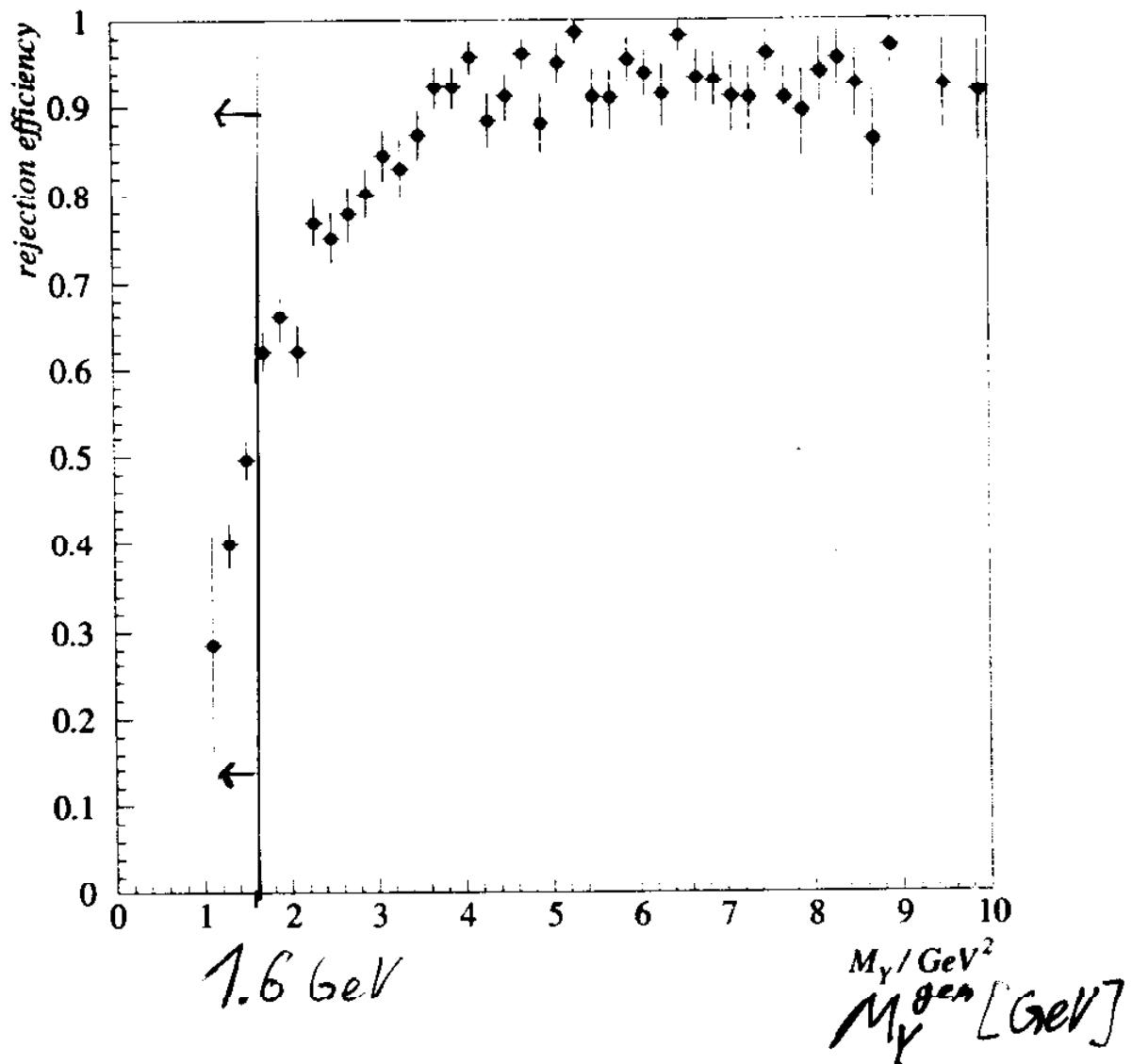
⇒ insures that system  $X$  is completely contained

⇒ measured cross section with

- $x_{IP} < 0.05$  (Y carries  $> 95\%$  of the proton momentum)
- $M_Y < 1.6 \text{ GeV}$  (→ see plot)

⇒ guided by data  
⇒ well defined on hadron level  
⇒ applicable to ANY kind of process

## Rejection Efficiency for Proton Dissociation



cross checked with various proton dissociation MCs

## Data and MC

### selection of data:

- selection of events with positrons ( $E > 8 \text{ GeV}$ ) and no signals in forward detectors
- additional cuts for rejection of background and to secure good resolution

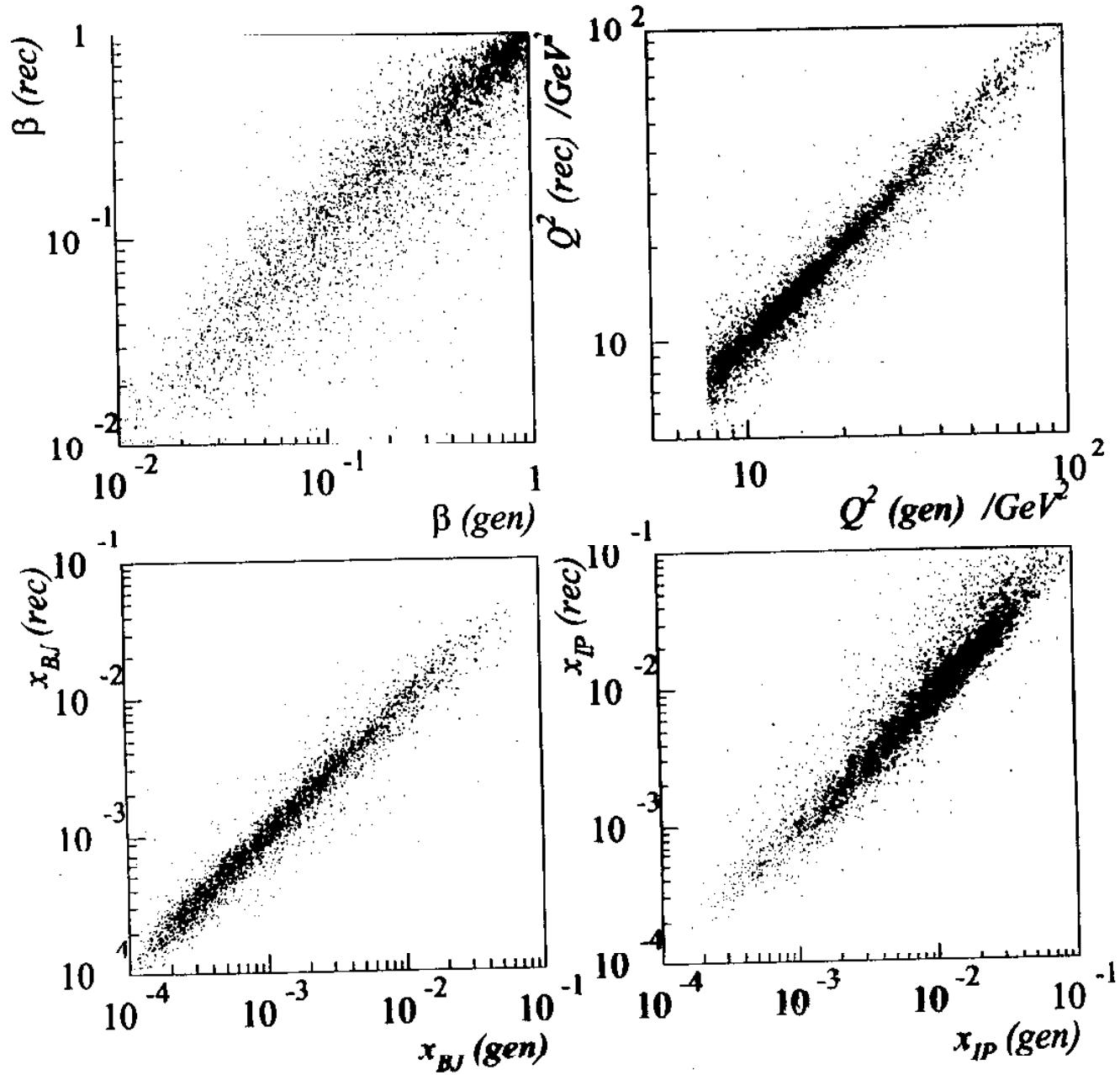
### correcting data for losses and smearing with MC mixture

- diffractive process : RapGap  $\pi^P$
- "standard"-DIS : DJANGO
- charge exchange : RapGap  $\pi^+$
- vector mesons : DIFFVM

(DJANGO and RapGap  $\pi^+$  are modelling the high  $x_P$  region  
the measurement is insensitive to whether  
DJANGO or RapGap  $\pi^+$  is used)

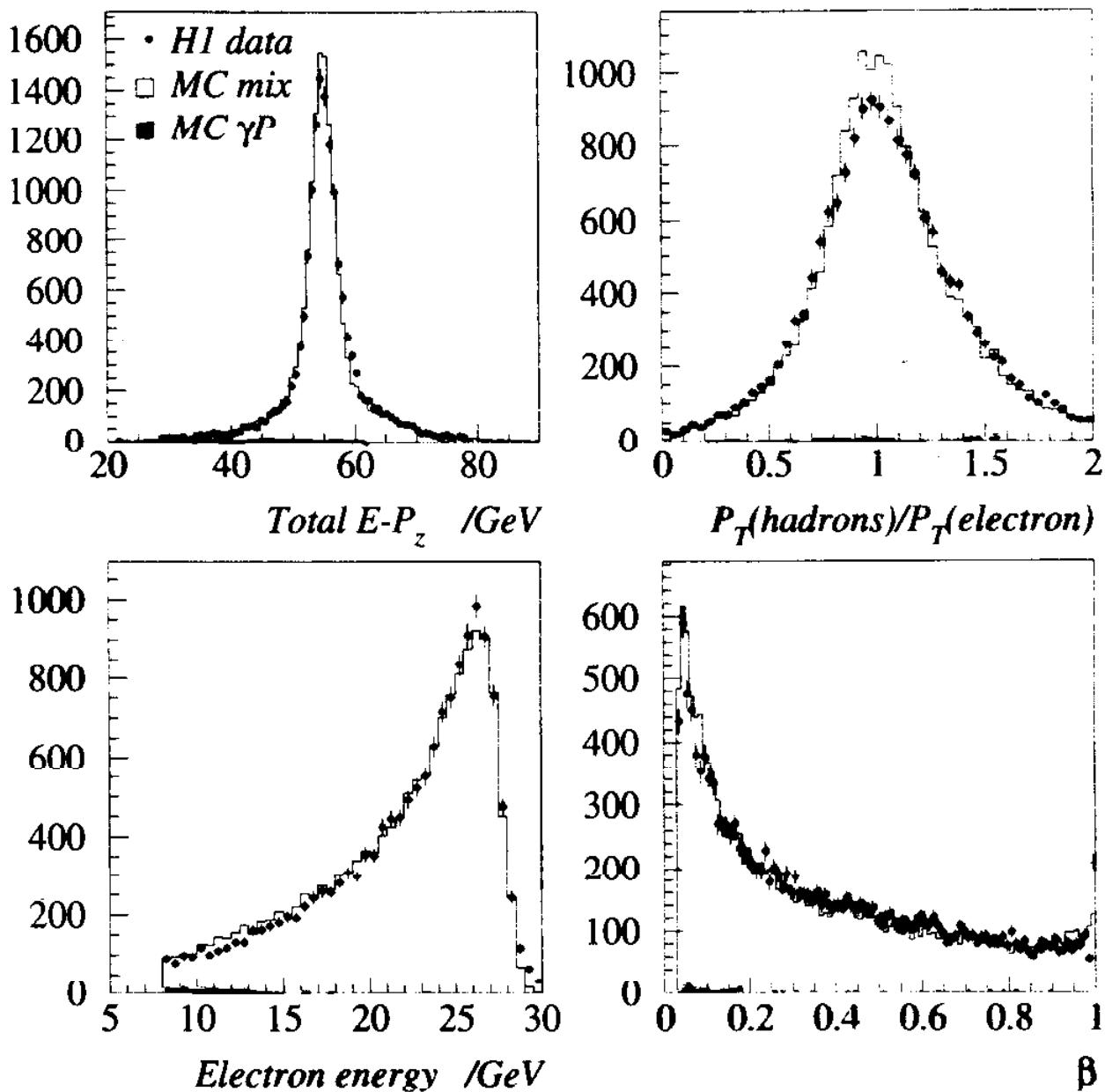
→ controlplots

## Reconstruction of Kinematic Quatities (from RAPGAP MC)



vnew

## Control Plots



## Diffractive Structurefunction $F_2^{D(3)}(x_P, \beta, Q^2)$

following Ingelman and Schlein

$$\frac{d^4\sigma_{ep \rightarrow e'XY}^D}{d\beta dQ^2 dx_P dt} = \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2(1+R)}\right) \cdot F_2^{D(4)}(Q^2, \beta, x_P, t)$$

- integration over  $|t_{min}| < |t| < 1 \text{ GeV}^2$
- set  $R = 0$

$$\frac{d^3\sigma_{ep \rightarrow e'XY}^D}{d\beta dQ^2 dx_P} = \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) \cdot F_2^{D(3)}(Q^2, \beta, x_P)$$

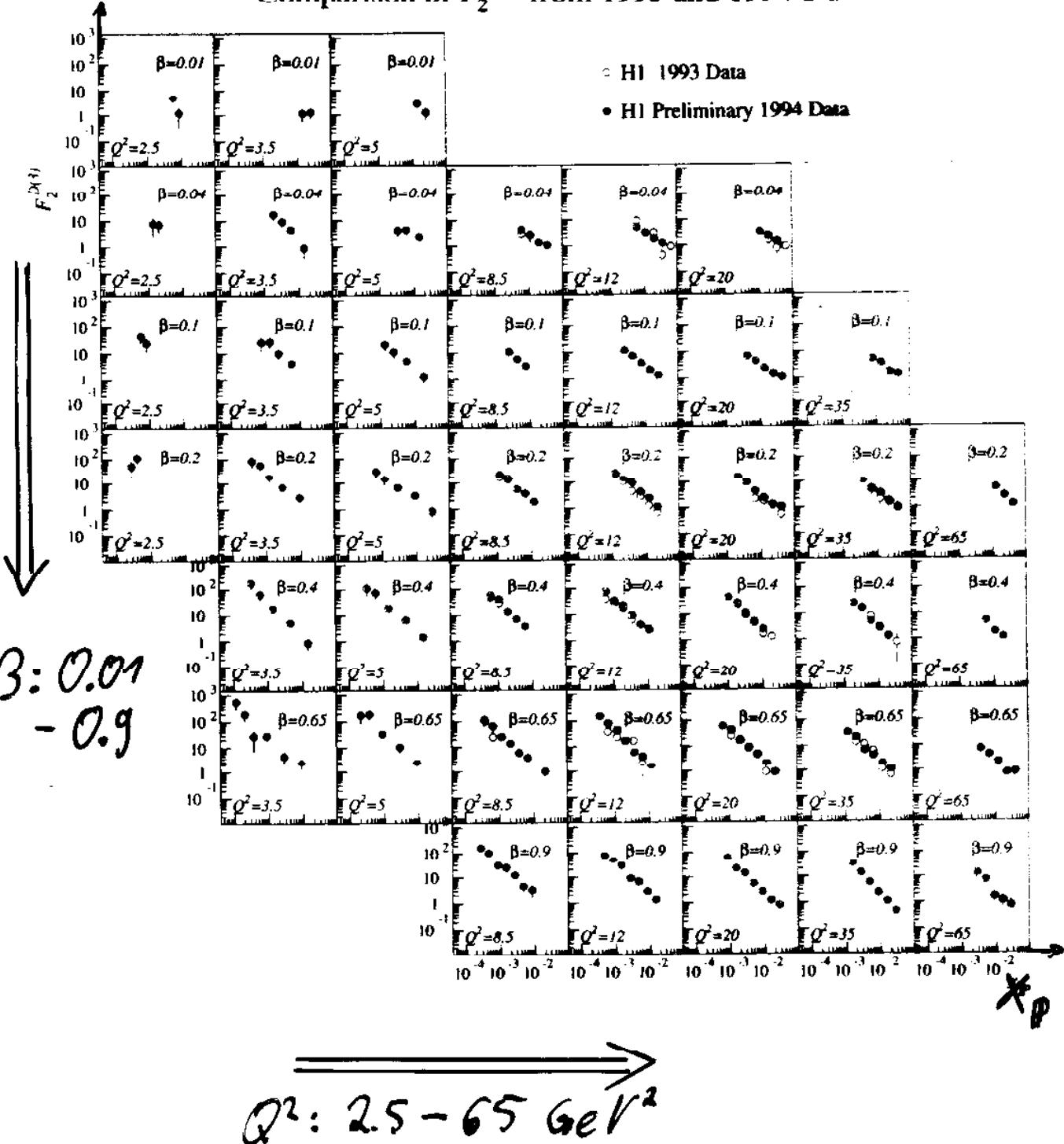
kinematic range:

$2.5 < Q^2 < 65 \text{ GeV}^2$
$0.01 < \beta < 0.9$
$0.0001 < x_P < 0.05$

# Measurement of $F_2^{D(3)}(x_{IP}, \beta, Q^2)$

$F_2^{D(3)}$

Comparison of  $F_2^{D(3)}$  from 1993 and 1994 Data

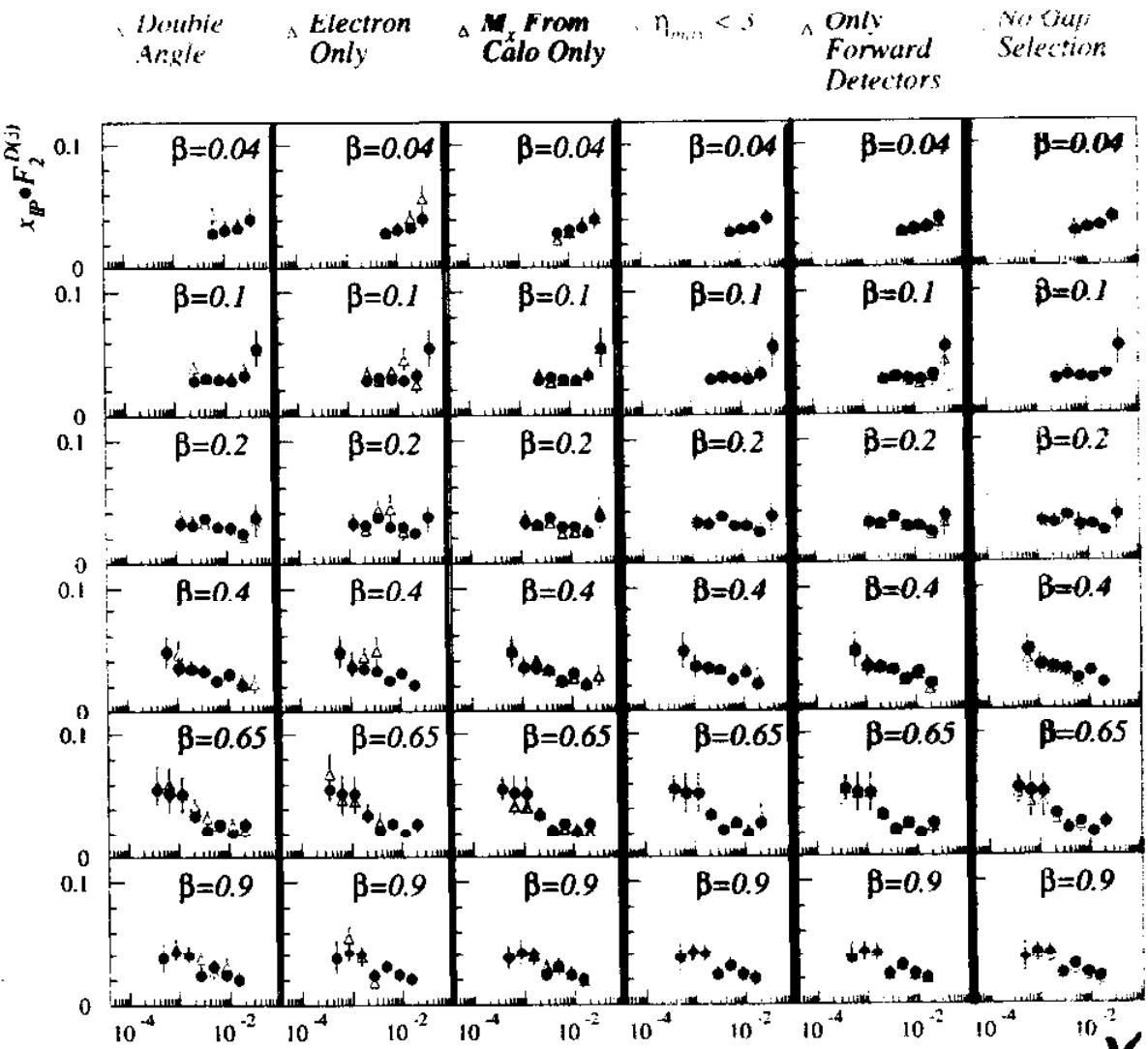


# Cross Check

H1 Preliminary data

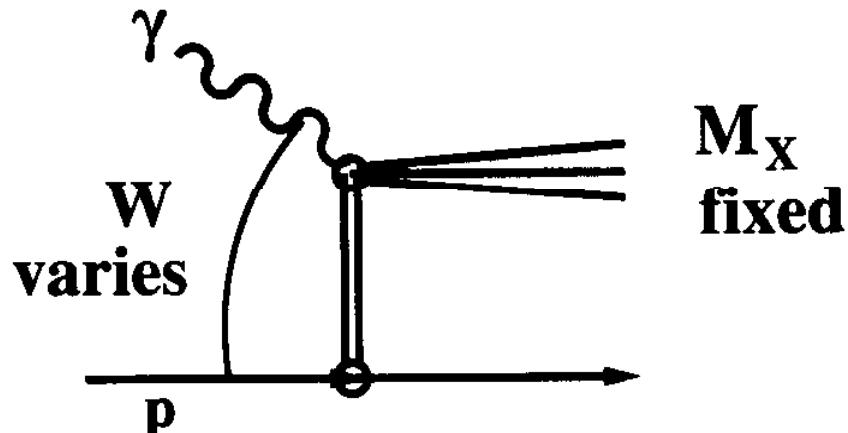
$$Q^2 = 12 \text{ GeV}^2$$

- Standard selection



- different selection and reconstruction methods
- correction to defined cross section  
⇒ results unchanged

## simple Regge picture



$$F_2^{D(3)}(x_{\mathbf{P}}, \beta, Q^2) = f_{\mathbf{P}/P}(x_{\mathbf{P}}) \cdot \tilde{F}_2^D(\beta, Q^2)$$

with  $f_{\mathbf{P}/P} \propto \frac{1}{x_{\mathbf{P}}^n} = \frac{1}{x_{\mathbf{P}}^{2\alpha(t)-1}}$

to test factorisation

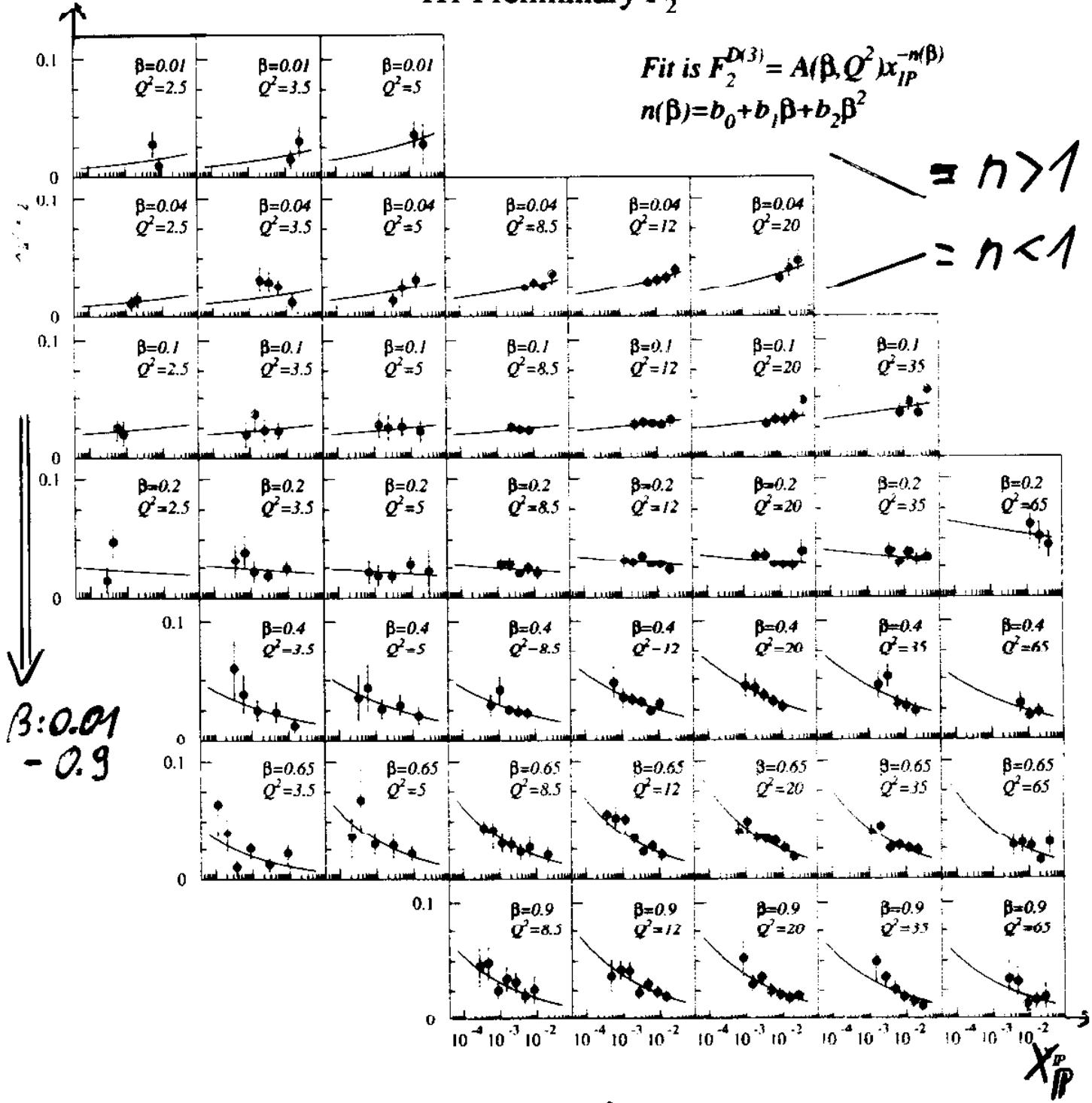
$$F_2^{D(3)}(x_{\mathbf{P}}, \beta, Q^2) = A(\beta, Q^2) \cdot \frac{1}{x_{\mathbf{P}}^n}$$

fit data with  $n = n(\beta)$  or  $n = n(Q^2)$

# Measurement of $F_2^{D(3)}(x_P, \beta, Q^2)$

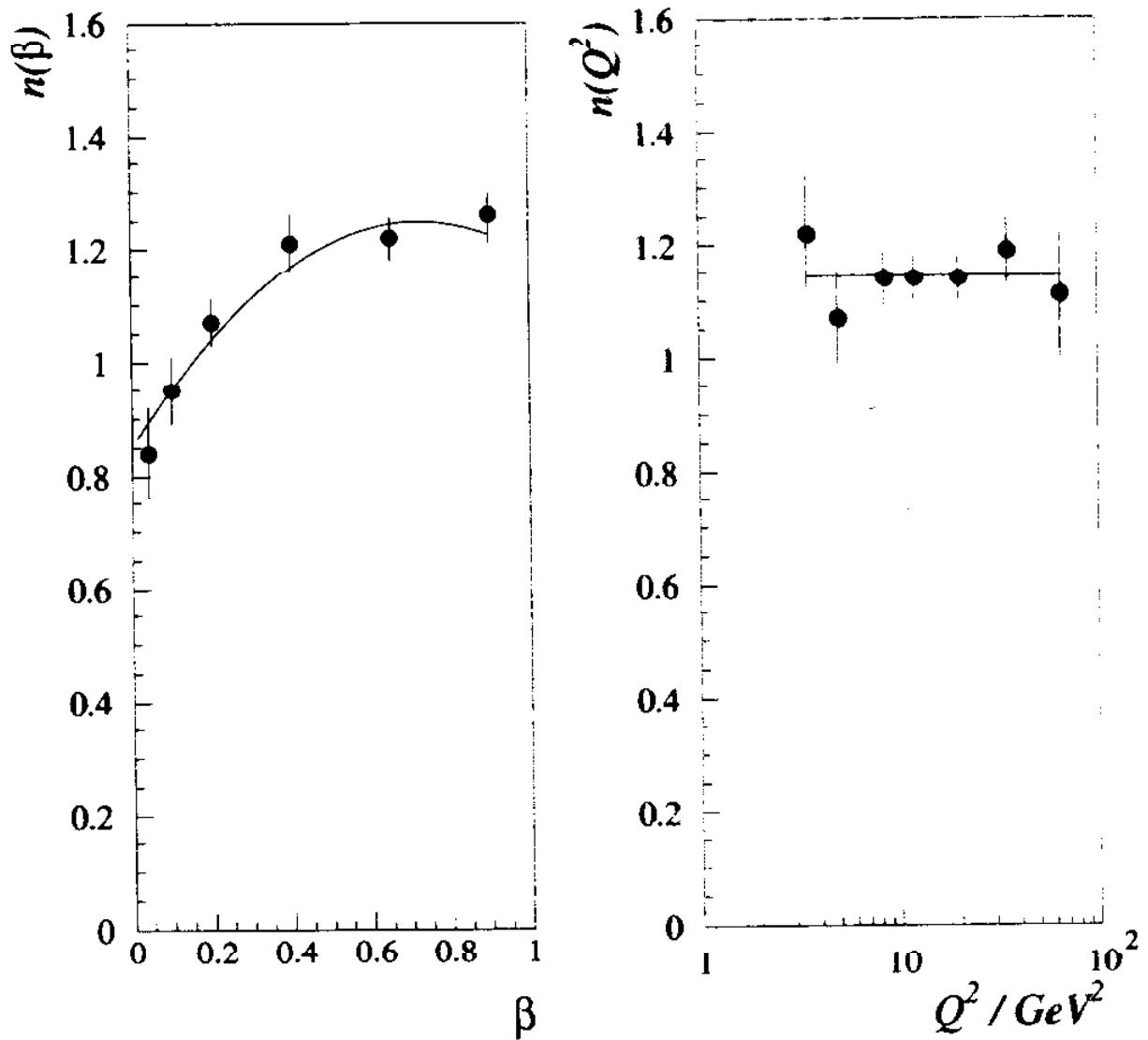
$x_P \cdot F_2^{D(3)}$

H1 Preliminary  $F_2^{D(3)}$



$\overrightarrow{Q^2: 2.5 - 65 \text{ GeV}^2}$

# Factorisation Breaking



- clear evidence for change of  $n$  with  $\beta$
- no dependence on  $Q^2$  visible

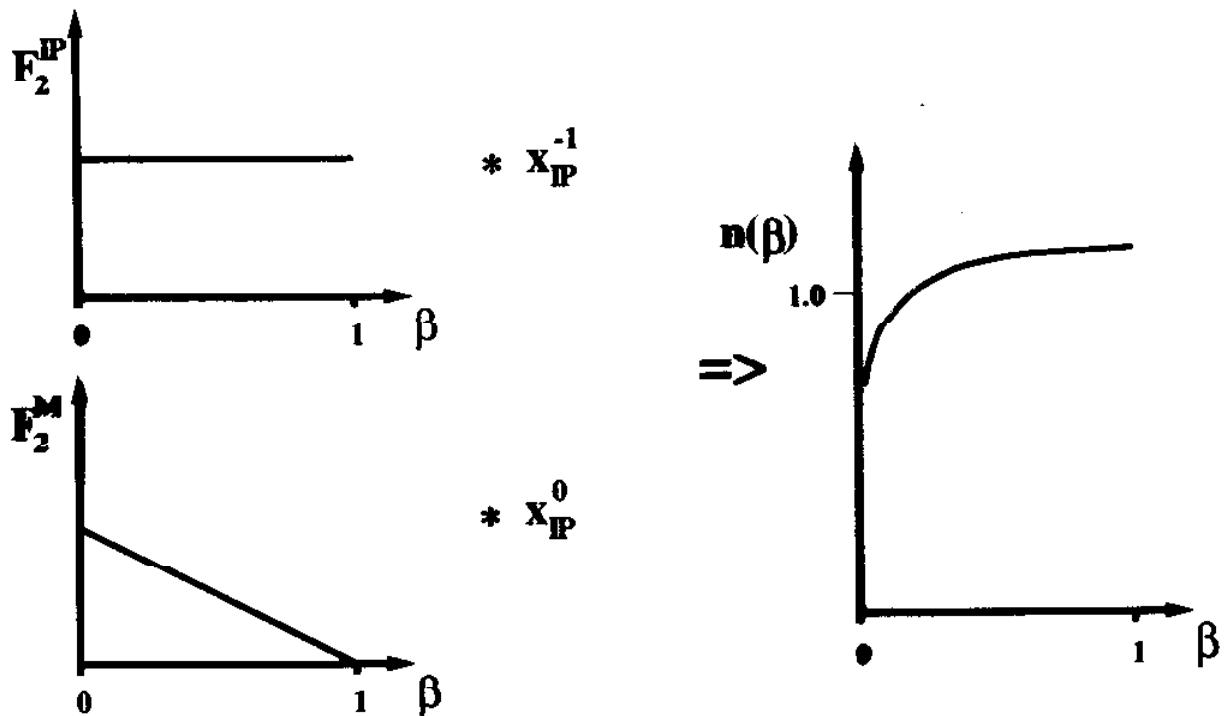
## Possible Explanation for Non-Factorisation

- subleading trajectory  $F_2^{D(3)}(x_P, \beta, Q^2) \propto \frac{1}{x_P^{2\alpha-1}} = \frac{1}{x_P^n}$

$$P \quad \alpha(0) \approx 1.1 \quad F_2^{D(3)} \propto x_P^{-1.2} \quad n \approx 1.2$$

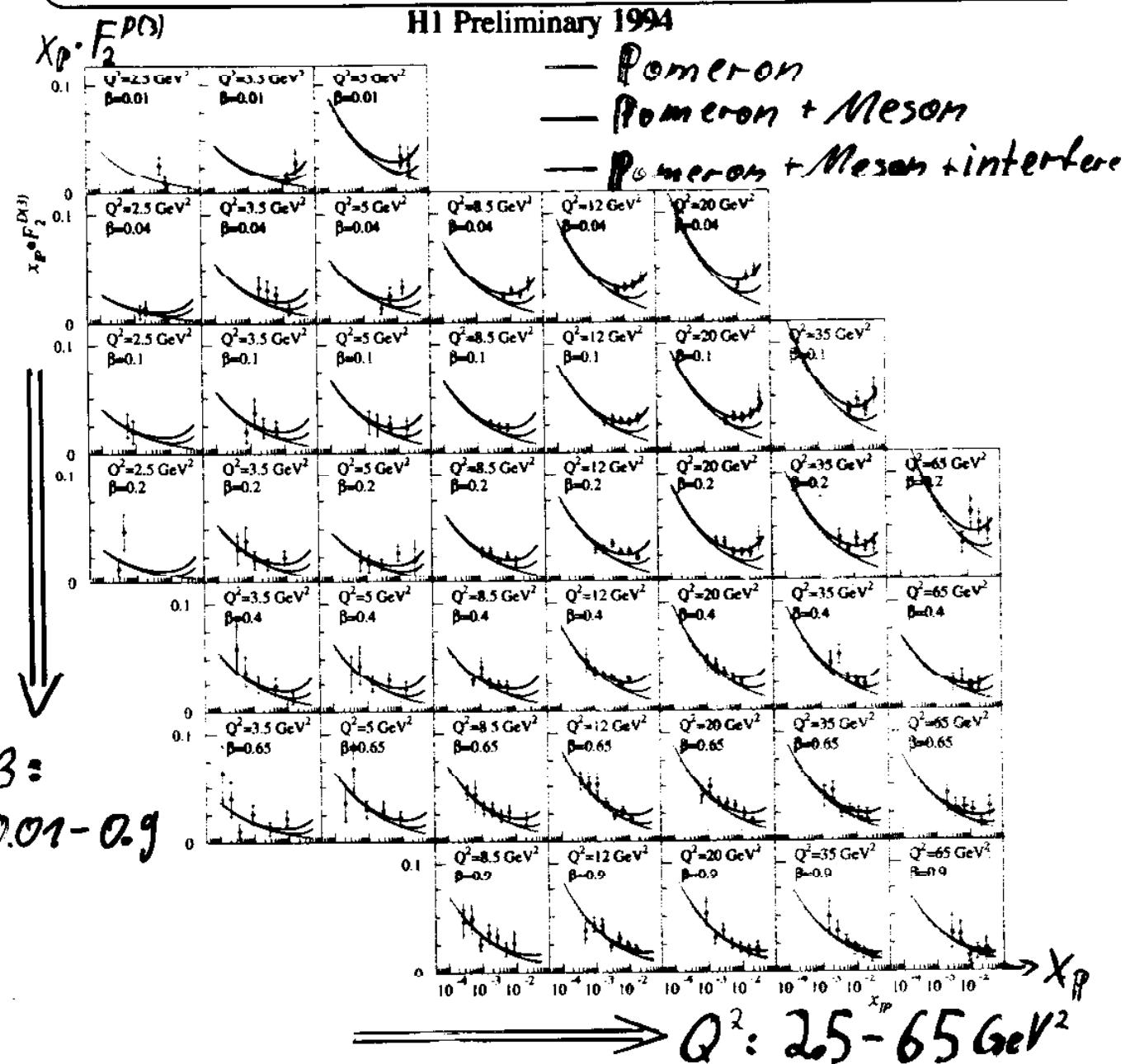
$$f_2, \dots \quad \alpha(0) \approx 0.5 \quad F_2^{D(3)} \propto x_P^0 \quad n \approx 0$$

$$\pi, \dots \quad \alpha(0) \approx 0.0 \quad F_2^{D(3)} \propto x_P^1 \quad n \approx -1$$



- non factorising Pomeron like in some perturbative models  
→ some models predict rising  $n$  for low  $\beta$
- ?

# Pomeron + Meson: Phenomenological Fit



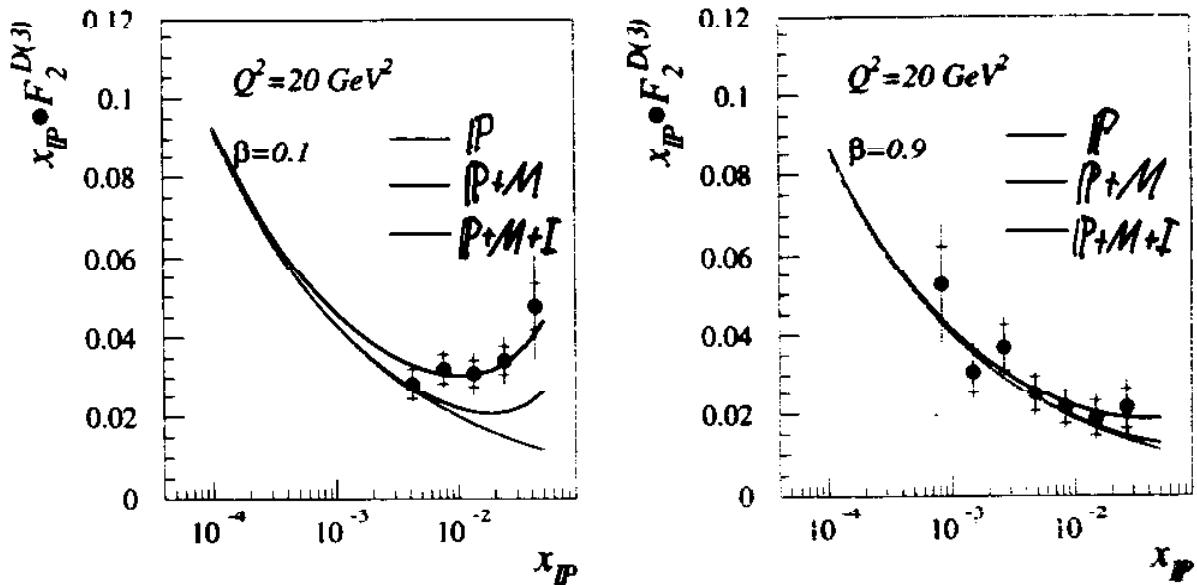
$$F_2^{D(3)}(x_P, \beta, Q^2) = \underline{F_2^P(\beta, Q^2) \cdot x_P^{-n_1}} + C_M \cdot \underline{F_2^M \cdot x_P^{-n_2}} + \underline{\text{int}_{45^\circ}}$$

fit of  $F_2^P(\beta, Q^2)$ ,  $n_1$ ,  $C_M$ ,  $n_2$

**Result:**  $n_1 = 1.29 \pm 0.03$     $\chi^2/ndf = 170/156$   
 $n_2 = 0.3 \pm 0.3$

# Pomeron + Meson

H1 Preliminary 1994



- large meson contribution at small  $\beta$  and high  $x_P$
- 50% meson intensity at low  $\beta$  and  $x_P = 0.05$
- few % meson intensity for  $x_P < 0.01$  or high  $\beta$
- large contribution of interference

here it becomes clear that it is important to measure a model independent cross section; we cannot make ad hoc assumptions on how the subleading contribution and the interference behave

## systematic error on $\alpha_P(0)$ and $\alpha_M(0)$

- covariance matrix for systematic errors on  $F_2^{D(3)}(x_P, \beta, Q^2)$
- allow any phase between  $0^\circ$  and  $90^\circ$
- meson structure:  $(1 - \beta)^{0.5}$  to  $(1 - \beta)^4$
- additional trajectory with  $n_3 = 0(\pi)$   
normalisation is consistent with zero

		stat	syst	model
<b>result:</b>	$n1 = 1.29$	$\pm 0.03$	$\pm 0.06$	$\pm 0.03$
	$n2 = 0.3$	$\pm 0.3$	$\pm 0.6$	$\pm 0.2$

### calculation of $\alpha_P(0)$ and $\alpha_M(0)$ :

assuming peripheral  $t$ -dependence ( $\propto e^{bt}$ )

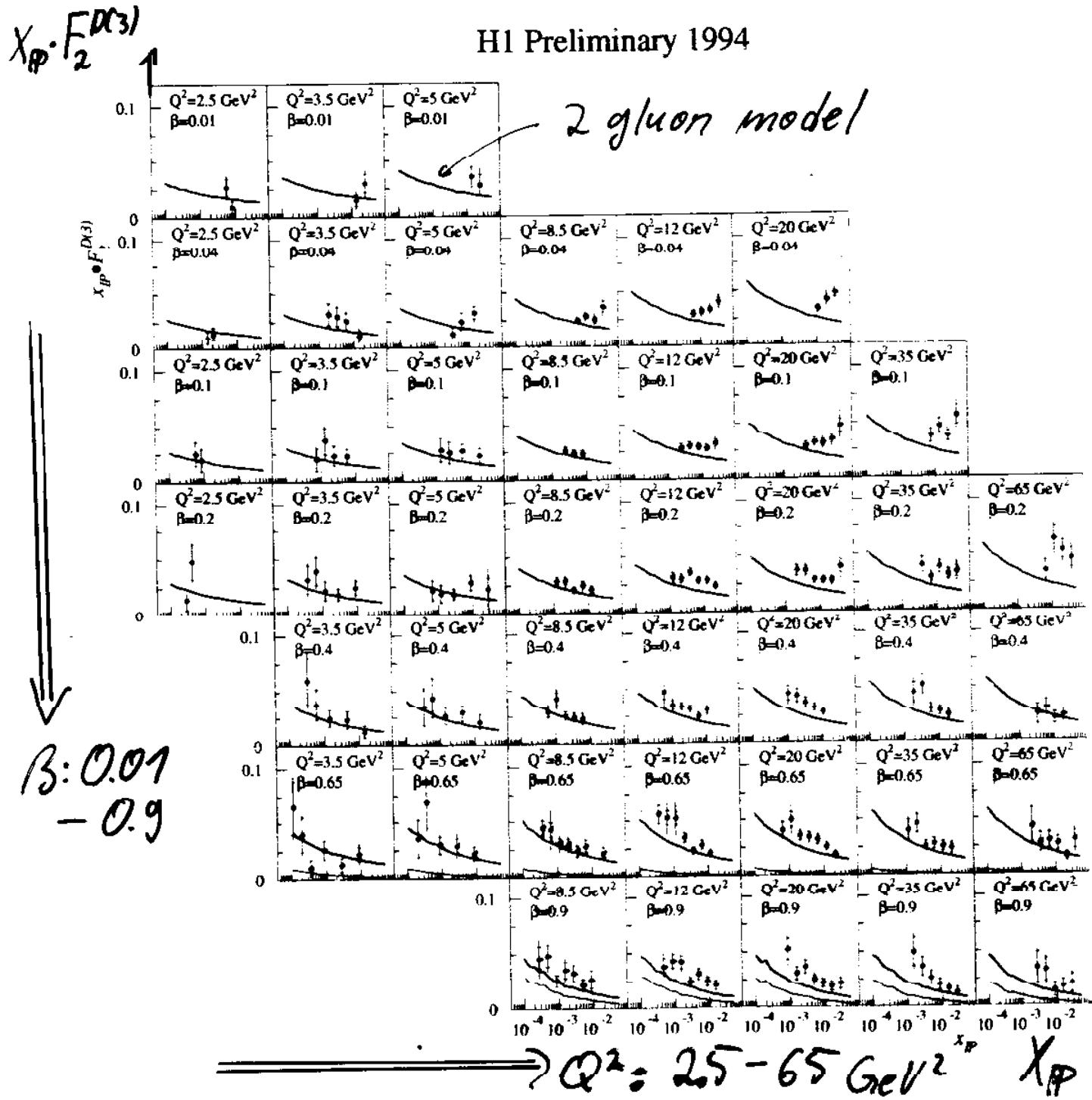
and linear trajectories  $\alpha(t) = \alpha(0) + \alpha' \cdot t$

assumptions	result
$\alpha'_M = 1, b_M = 5$	$\alpha_M(0) = 0.6 \pm 0.1 \pm 0.3$
$\alpha'_P = 0$	$\alpha_P(0) = 1.15 \pm 0.02 \pm 0.04$
$\alpha'_P = 0.3, b_P = 6$	$\alpha_P(0) = 1.18 \pm 0.02 \pm 0.04$

## 2-Gluon Exchange Model

Hard pomeron model in which energy dependence and normalisation are determined by gluon distribution in proton  
 (M. Wüsthoff, J. Bartels)

Other models give similar result → overview in paper by  
 M.C. McDermont and G. Briskin (HEP-PH 9610245)



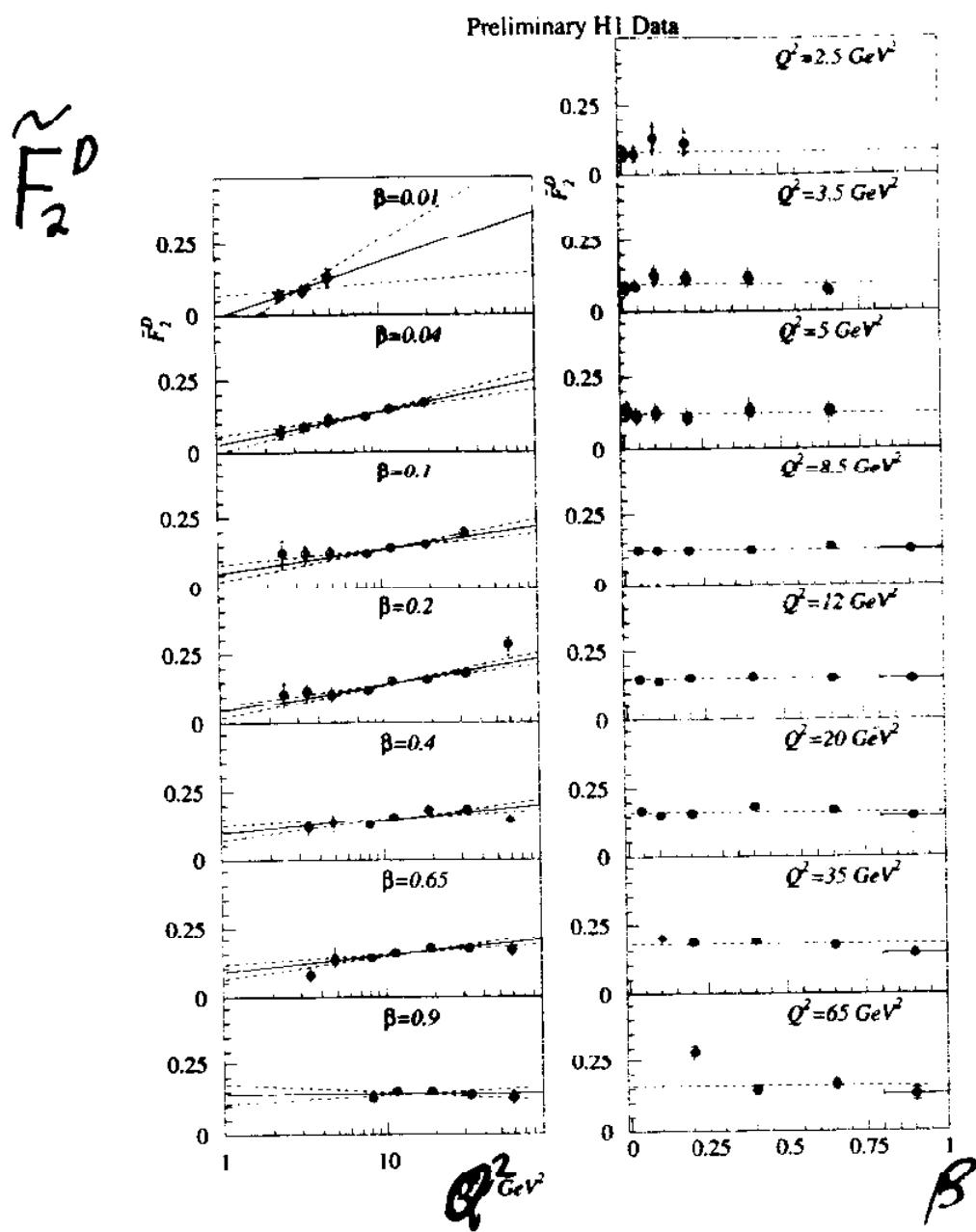
## Determination of $\tilde{F}_2^D(\beta, Q^2)$

$$\tilde{F}_2^D(\beta, Q^2) = \int_{x_{PL}}^{x_{PH}} F_2^{D(3)}(x_P, \beta, Q^2) dx_P$$

- $x_{PL} = 0.0003$  and  $x_{PH} = 0.05$ : near experimental limits
- $F_2^{D(3)}(x_P, \beta, Q^2)$ -parameterisation is used to extrapolate into non-measured region  
in factorisation models:

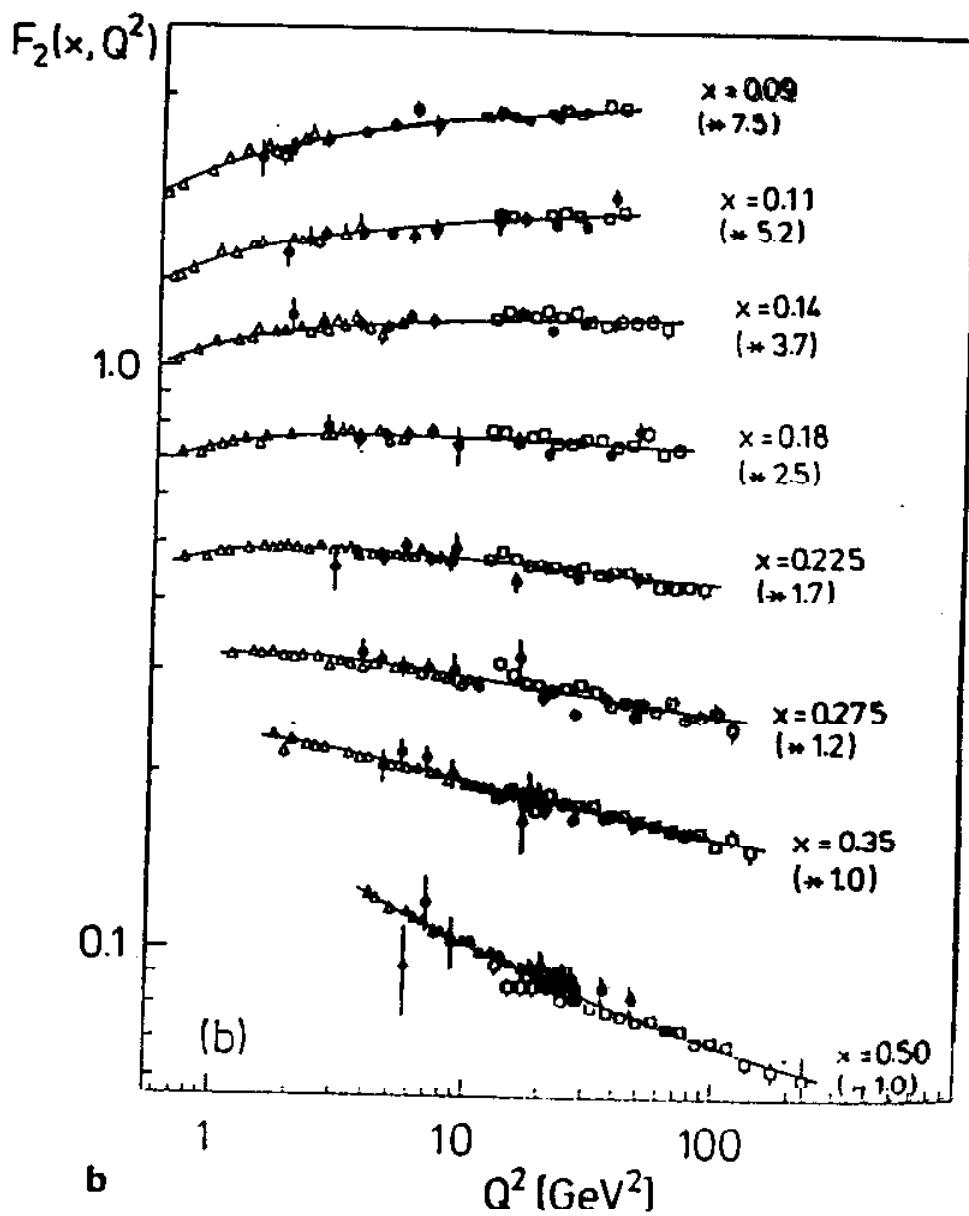
$$\tilde{F}_2^D(\beta, Q^2) \propto F_2^P(\beta, Q^2)$$

$\Rightarrow \tilde{F}_2^D(\beta, Q^2)$  can be used to study scaling properties



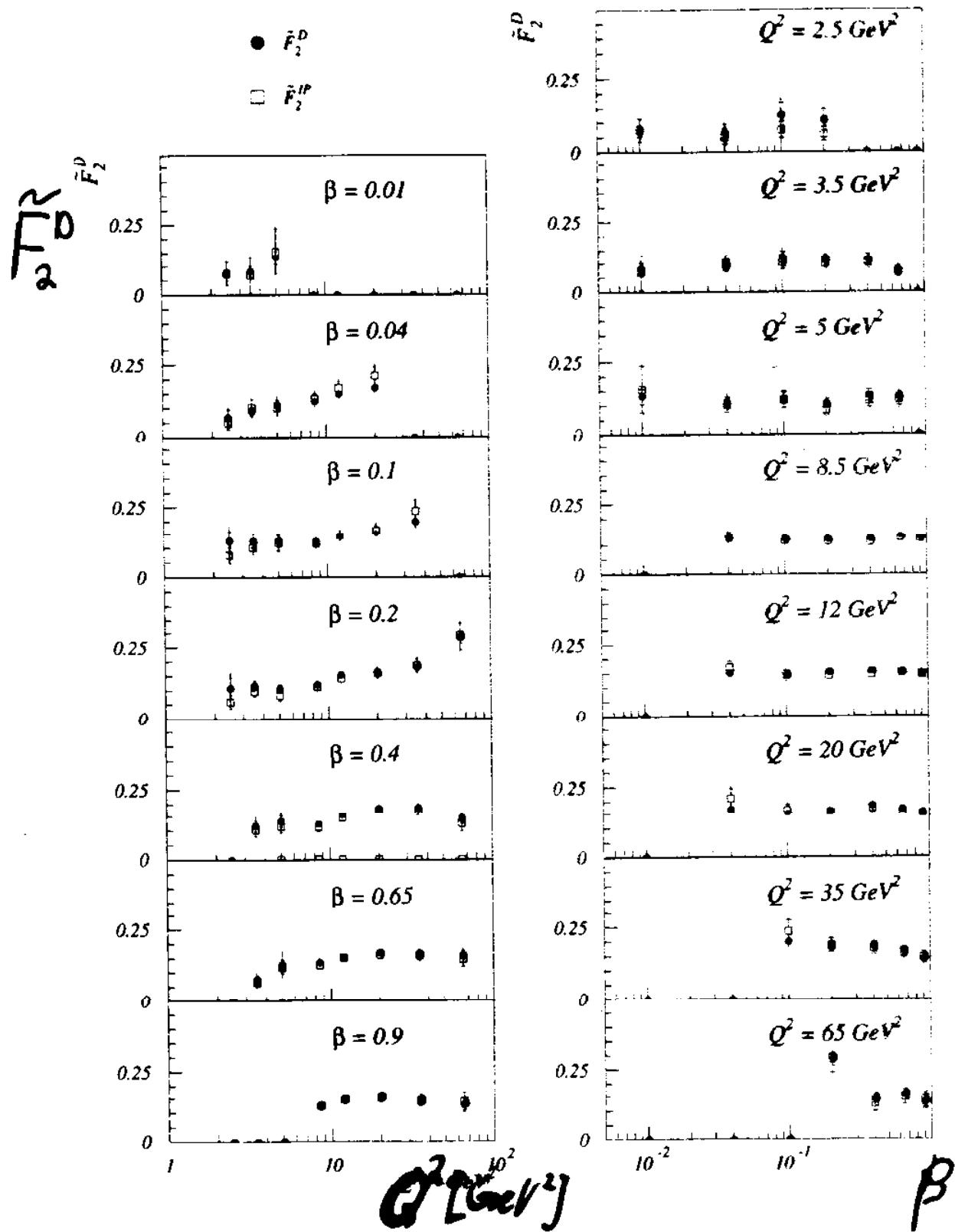
- rise in  $\log(Q^2)$  even to high  $\beta$  ;  
not seen in  $F_2^{\text{Proton}}$   $\rightarrow$  evidence for gluons at high  $\beta$ ?
- approximately flat in  $\beta$
- calculation with  $\tilde{F}_2^D(\beta, Q^2)_{x_P < 0.01}$  and  $F_2^P(\beta, Q^2)$   
(Pomeron part of fit) give consistent result

$\beta$   
 $F_2^{\text{Proton}}(x, Q^2)$



# Influence of Meson Exchange

H1 Preliminary 1994



## **QCD-Analysis**

**Q:** Can DGLAP describe  $\tilde{F}_2^D(\beta, Q^2)$  and quantify the qualitative conclusion from the scaling violations?

various theoretical predictions:

- DGLAP should not work at all
  - DGLAP should be OK, but fail at  $\beta \rightarrow 1$
- ⇒ no consensus

**Experimentally look for failure of DGLAP!**

**Results:**

- DGLAP seems to be ok, but does that mean anything?  
Do we really see consequences of 'leading gluon' in final state?  
Or is DGLAP just a good parameterisation?
- look at charm, topology, . . .

# **QCD-Analysis of $\tilde{F}_2^D(\beta, Q^2)$ in LO**

- consider light flavour singlet and gluon
- parametrise parton density at  $Q_0^2 = 2.5 \text{ GeV}^2$ :  
$$\beta f_i(\beta) = A_i \beta^{B_i} (1 - \beta)^{C_i}$$
- solve DGLAP evolution to evolve parton densities
- fit  $A_i$ ,  $B_i$  and  $C_i$  to data (i=singlet,gluon)
  - charm included via photon-gluon fusion  
no momentum sum rule imposed

## **two scenarios:**

- only quarks at  $Q_0^2 \Rightarrow A_{\text{gluon}} = 0$
- quarks and gluons present at  $Q_0^2$

## **cross checks:**

- analysis done with  $\tilde{F}_2^D(\beta, Q^2)_{x_P < 0.05/0.01}, \tilde{F}_2^P$
- two DGLAP evolution programs: working in  $x_{Bj}$ -space and using Mellin transformation method
- result of H1 QCD analysis of 1993 data has been reproduced by several independent theoretical groups

# ONLY Quarks at $Q_0^2 = 2.5 \text{ GeV}^2$

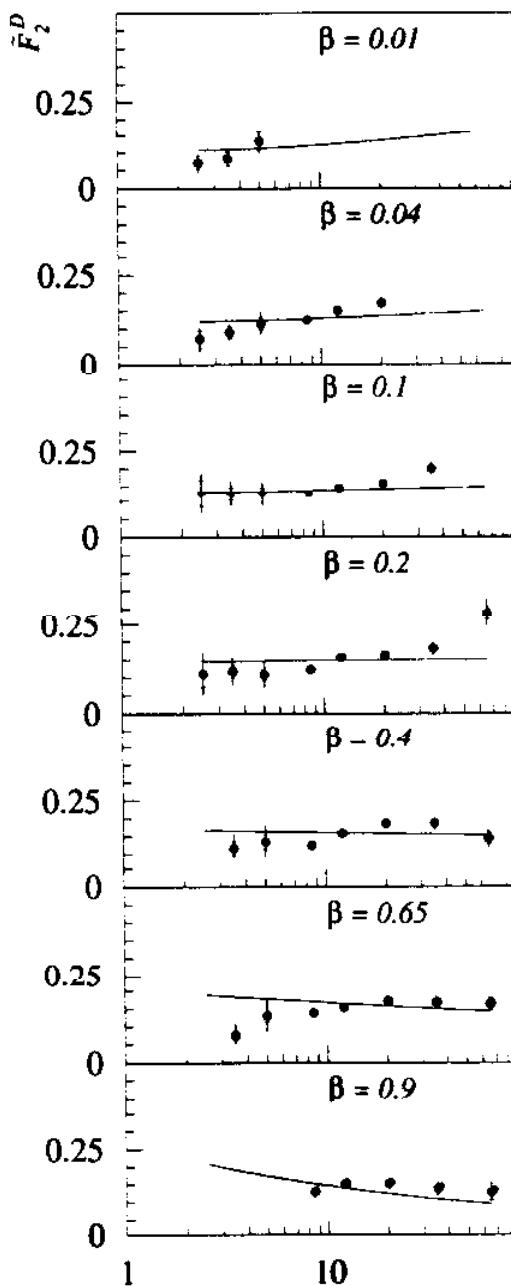
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*QCD Fit*

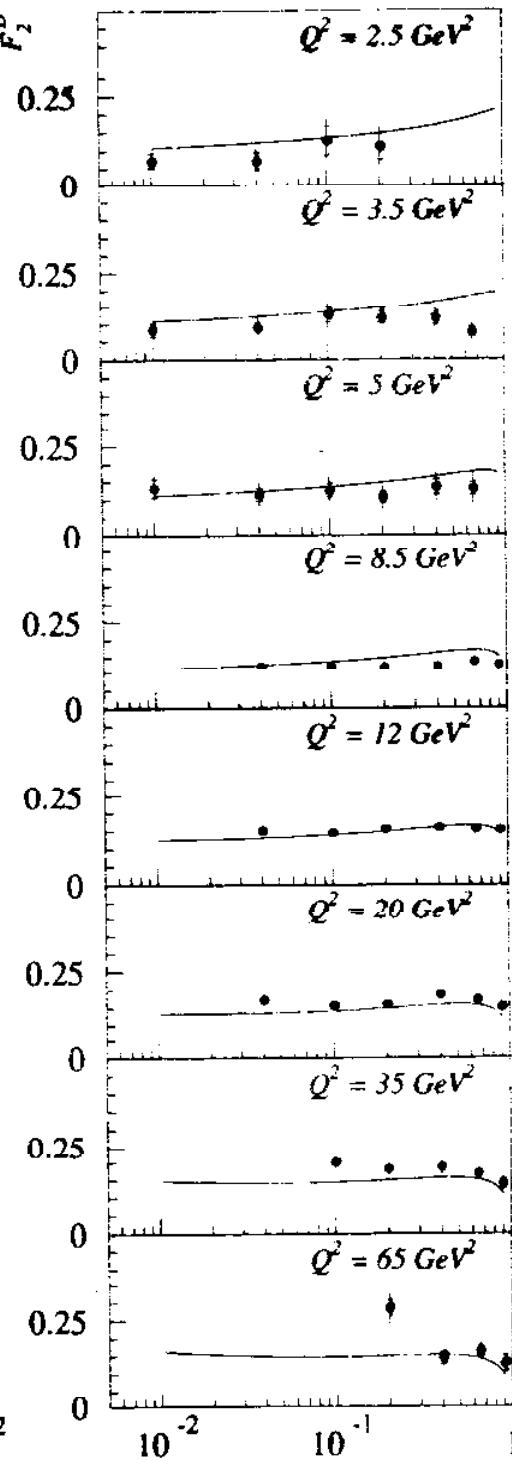
*Quarks Only,  $Q_0^2 = 2.5 \text{ GeV}^2$*

$\chi^2/ndf = 95.2/39$

$\tilde{F}_2^D$



$\tilde{F}_2^D$



$Q^2 [\text{GeV}^2]$

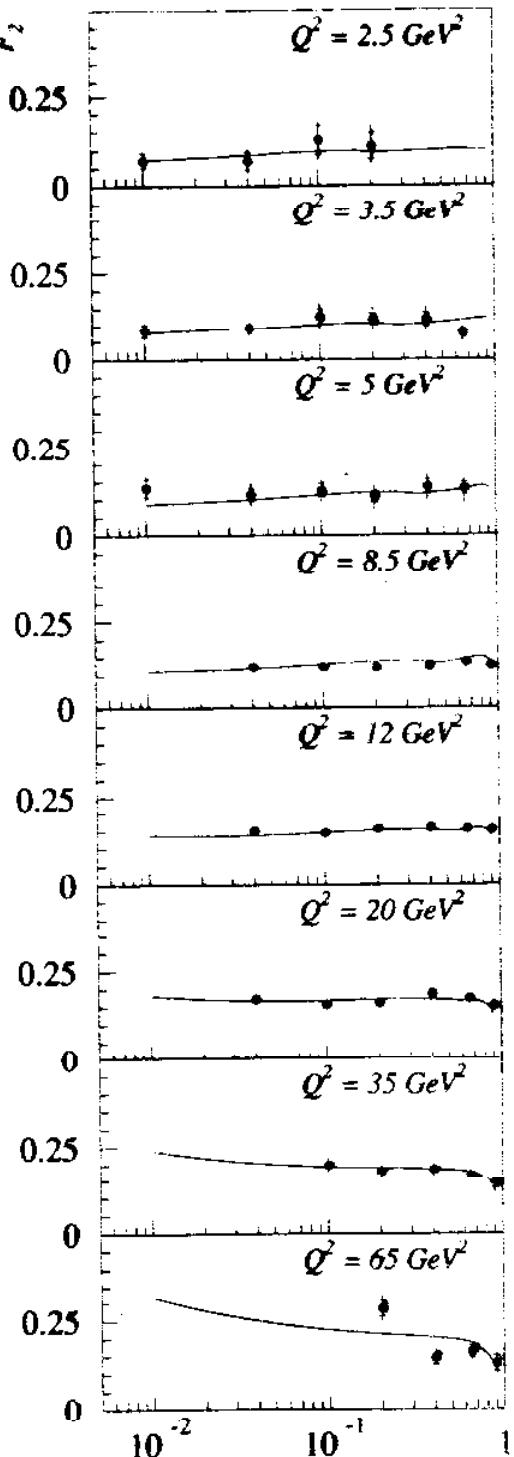
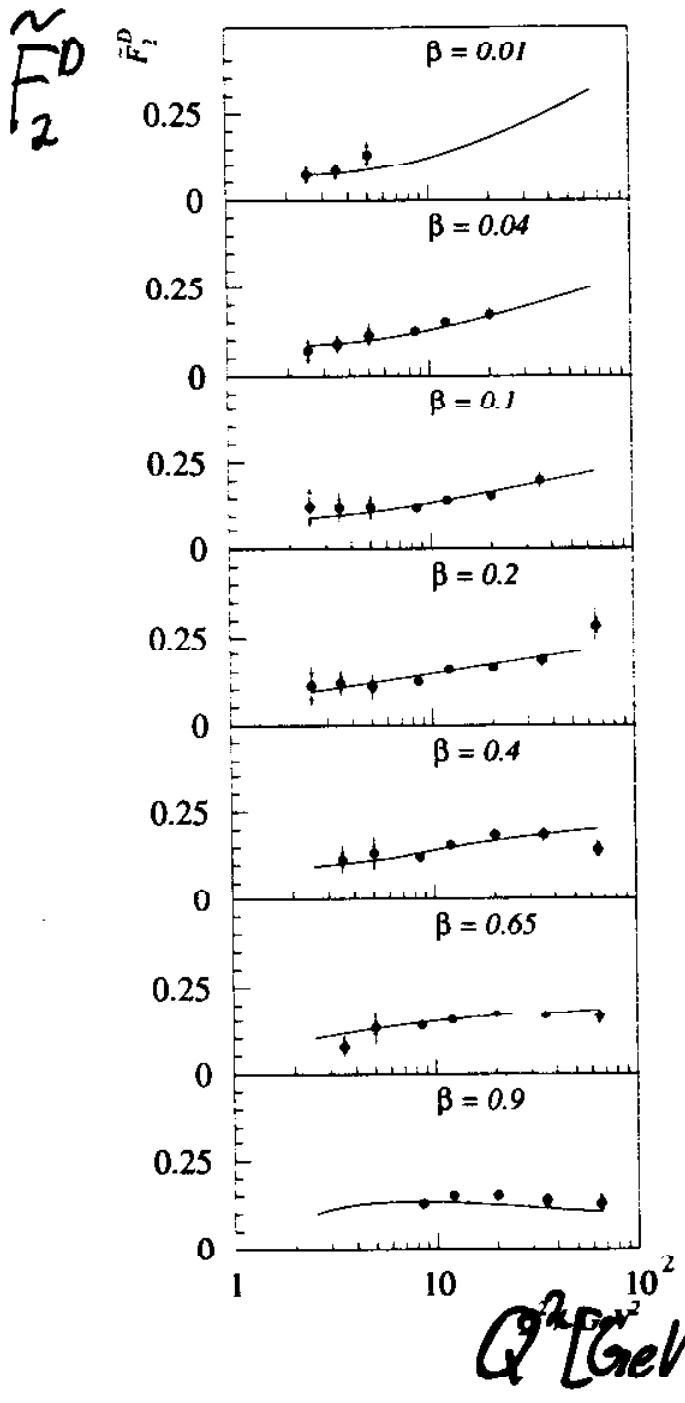
$\beta$

# Quarks and Gluons at $Q_0^2 = 2.5 \text{ GeV}^2$

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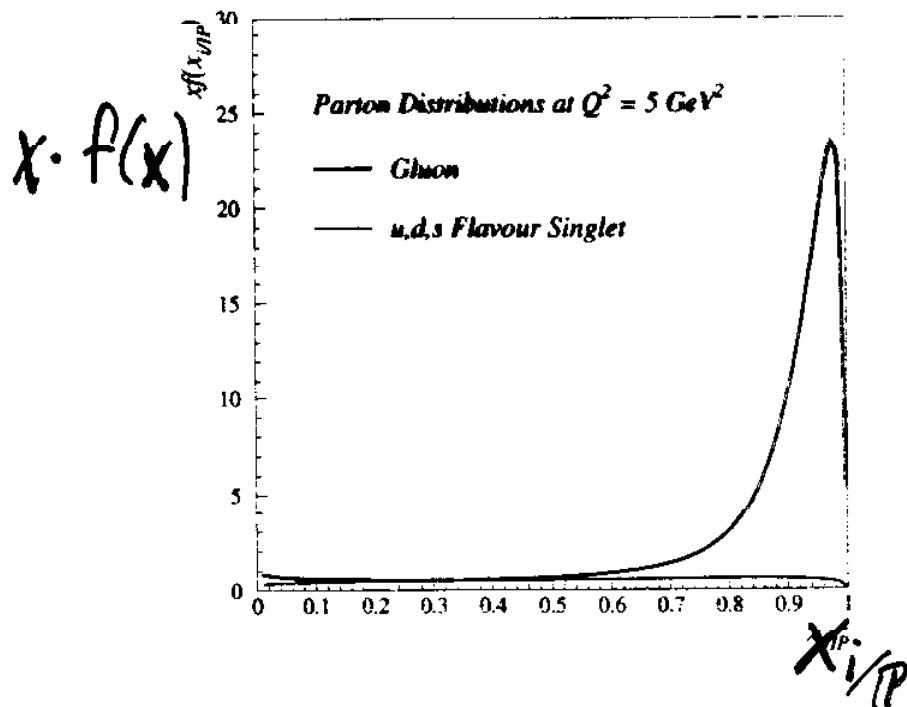
*QCD Fit*

Quarks + Gluons,  $Q_0^2 = 2.5 \text{ GeV}^2$   
 $\chi^2/\text{ndf} = 36.8/37$

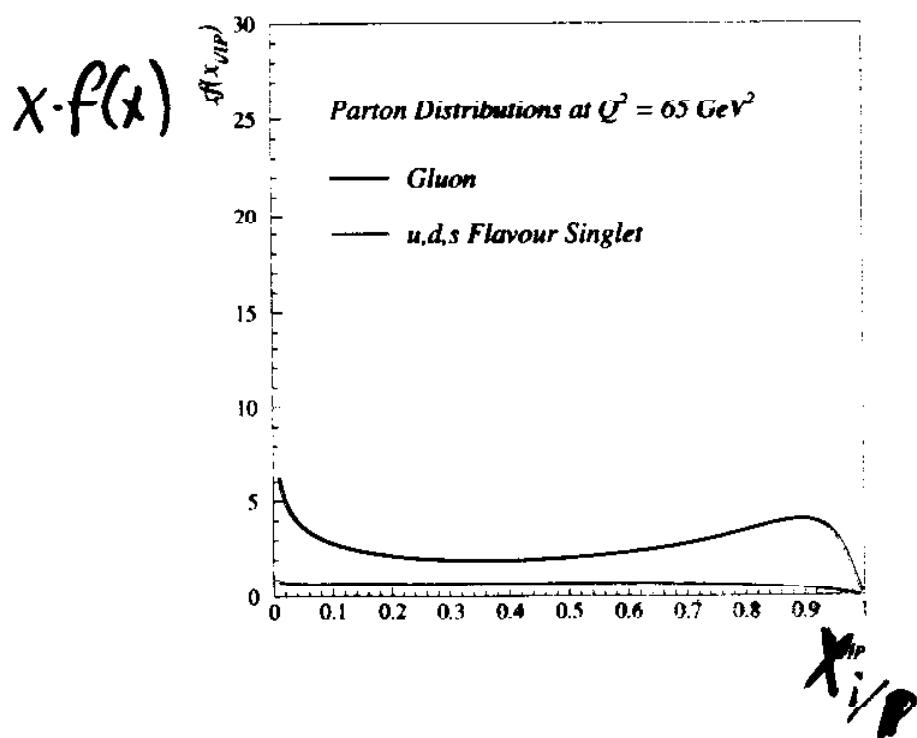


# Parton Distribution Functions

H1 Preliminary 1994



H1 Preliminary 1994



## Summary/Conclusions/Outlook

- $F_2^{D(3)}(x_P, \beta, Q^2)$  has been measured over a wider kinematic range and to better precision
- evidence for factorisation breaking in  $\beta$   
⇒ possible explanation of breaking: subleading trajectory
- $\tilde{F}_2^D(\beta, Q^2)$  is flat in  $\beta$
- scaling violations observed which hint for gluon dominance
- QCD-fit results in 'leading' gluon structure
- more insight into hadronic structure by looking into hadronic final state: talk on Wednesday
- soon measurement of  $F_2^{D(3)}(x_P, \beta, Q^2)$  for lower  $Q^2$